

1195. Proposed by Mike Pinter, Belmont University, Nashville, TN.

Consider the following alphanumeric: $MCCAIN + OBAMA = DECIDE$. As we cast our vote, we want to maximize our decision. Find the maximum value of DECIDE for the alphanumeric.

Solution by the Armstrong Problem Solvers, Armstrong Atlantic State University, Savannah, GA.

The maximum value of DECIDE is 418041, with solution $388506 + 29535 = 418041$.

From the leftmost column we must have $D = M + 1$ and, from the tens column, I must be 0 or 1. Since no digit is carried to the hundreds column, I must be even, and hence $I = 0$. That means $A = 5$ and, from the thousands column, $B = 9$. Since a 1 must be carried to the tens column, $N + 5 = E + 10$, and $N = E + 5$. Thus, E must be 1, 2, or 3, and N must be 6, 7, or 8. Since a 1 must be carried to the ten thousands column, $C + O + 1 = E + 10$, and $C + O = E + 9$.

If $E = 3$, then $N = 8$ and $C + O = 12$, so $\{C, O\}$ must be $\{3, 9\}$, $\{4, 8\}$, or $\{5, 7\}$, each of which is impossible, since $B = 9$, $N = 8$, and $A = 5$. If $E = 2$, then $N = 7$ and $C + O = 11$, so $\{C, O\}$ must be $\{3, 8\}$ since $B = 9$, $N = 7$, and $A = 5$, leaving $\{M, D\} \subset \{1, 4, 6\}$, which is impossible, since $D = M + 1$. Therefore, we must have $E = 1$, $N = 6$, and $C + O = 10$, so $\{C, O\}$ must be $\{2, 8\}$, or $\{3, 7\}$. If $\{C, O\} = \{3, 7\}$, then $\{M, D\} \subset \{2, 4, 8\}$, which is again impossible, since $D = M + 1$. Thus, $\{C, O\} = \{2, 8\}$, $M = 3$, and $D = 4$. Of the two possible solutions, the larger value of $DECIDE$ occurs when $C = 8$ and $O = 2$.

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